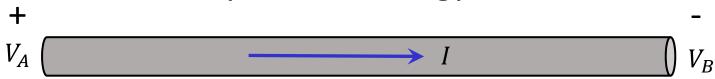


In the hydraulic analogy, electrical circuits are considered analogous to:

- [A] buckets of water
- [B] water flowing through pipes
- [C] water molecules subjected to heat, stirring and turbulence
- [D] hydroelectric ocean waves
- [E] I don't know

## Hydraulic analogy



'the flow of particles'

'what pushes'

Relationship between the push and the flow

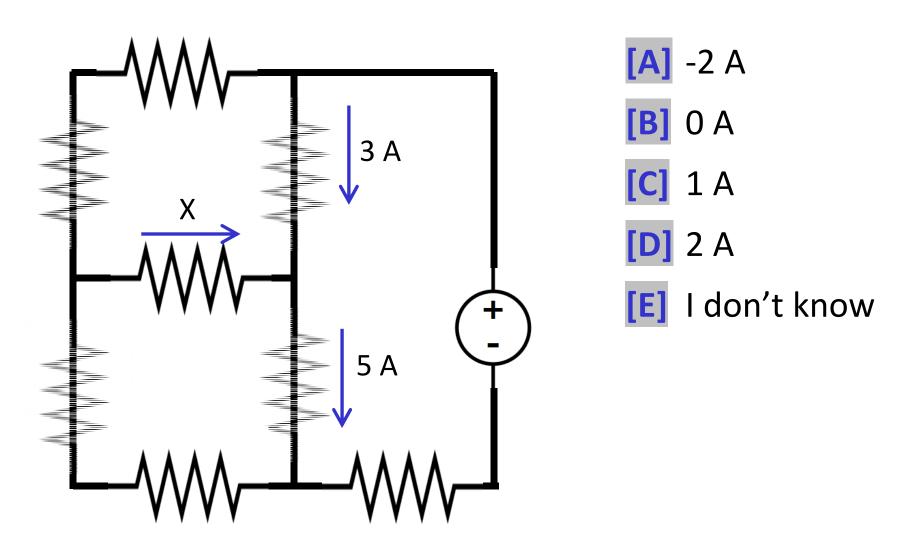
Physical quantity	symbol	units
current	I i	ampere (A)
pressure/voltage	V = v	volts (V)
resistance	R	ohm (Ω)

$$V = I \cdot R$$
 Ohm's Law

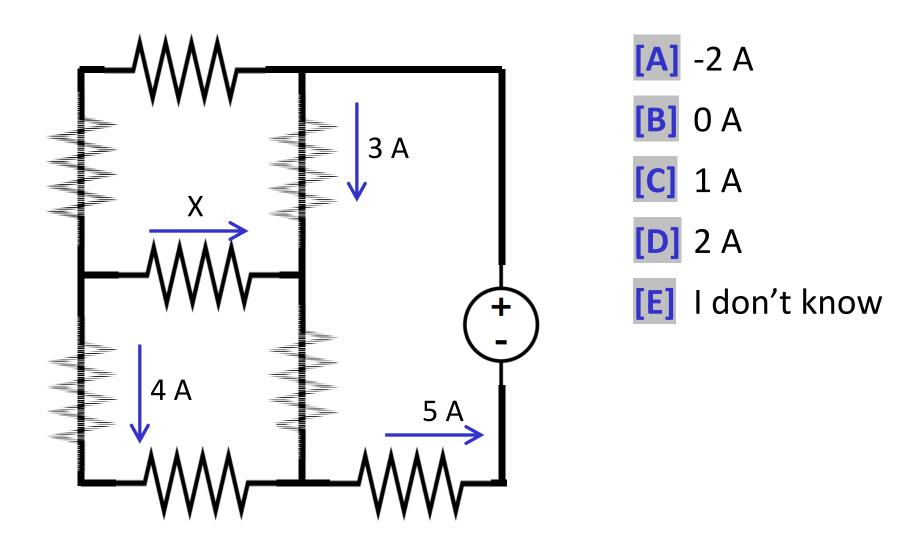
$$\sum_{i=1}^{n} I = \sum_{i=1}^{n} I$$
 Kirchhoff's Current Law (KCL)

$$\sum_{v} \Delta V = \sum_{down} \Delta V$$
 Kirchhoff's Voltage Law (KVL)

If the currents in the various pipes are measured as indicated on the arrows, what is the value of the unknown current X?



If the currents in the various pipes are measured as indicated on the arrows, what is the value of the unknown current X?

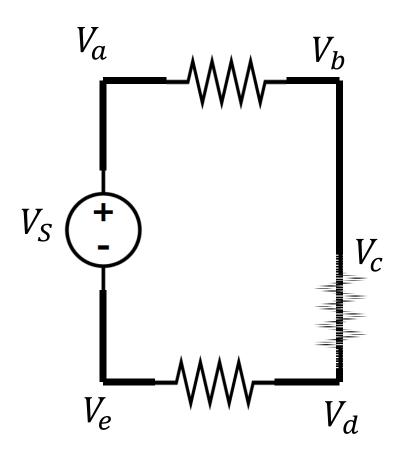


$$V_a - V_b = 1 V$$

$$V_d - V_e = 2 V$$

$$V_S = 5 V$$

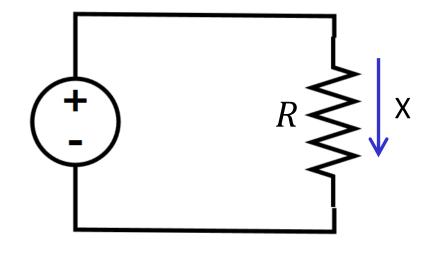
What is the voltage  $(V_c - V_d)$ ?



- [D] Not enough info to calculate
- [E] I don't know

If the resistance R of the pipe is 2  $\Omega$ , the current X is:

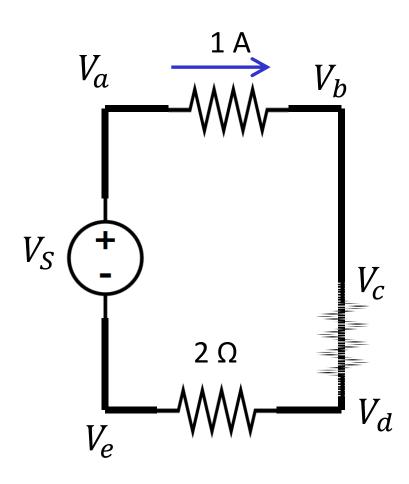
$$V_{S} = 8 V$$



$$V = I \cdot R$$

$$V_a - V_b = 4 V$$
$$V_S = 10 V$$

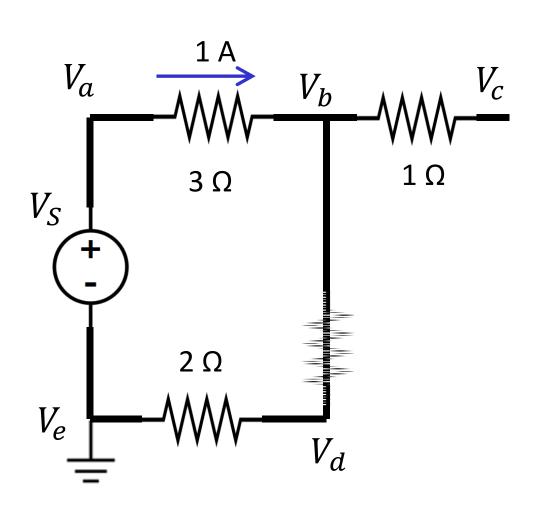
What is the voltage  $(V_c - V_d)$ ?



- [A] 2 V
- [B] 4 V
- [C] 6 V
- [D] Something else
- [E] I don't know

$$V_S = 10 V$$

What is the value of node voltage  $V_c$ ?



- [A] 0 V
- [B] 4 V
- [C] 6 V
- [D] 7 V
- [E] I don't know

If the resistance  $R_1$  of the first pipe is 2  $\Omega$  and the resistance  $R_2$  of the second pipe is 4  $\Omega$ , the following is true:

$$V_S = 8 V$$

$$R_1 R_2$$

$$I_1 I_2$$

 $V = I \cdot R$ 

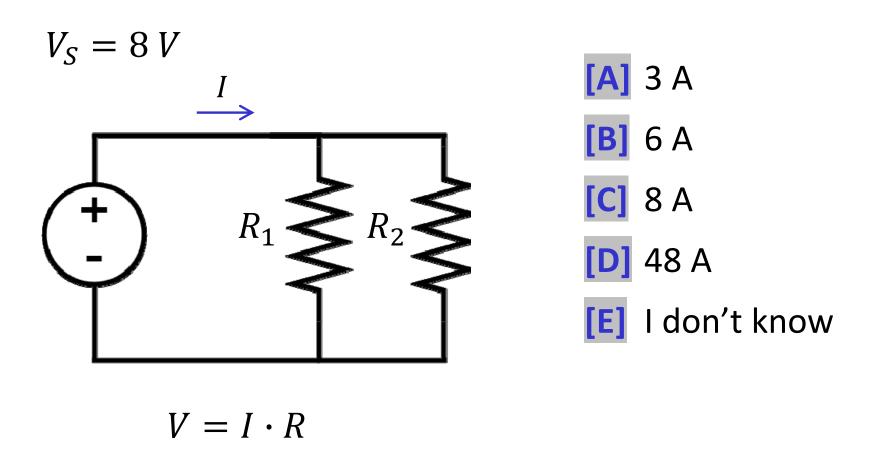
[A] 
$$I_1 = I_2 = 0$$

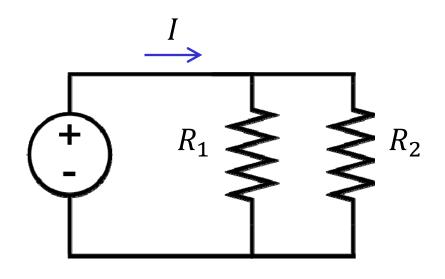
[B] 
$$I_1 = I_2 > 0$$

[C] 
$$I_1 > I_2$$

[D] 
$$I_1 < I_2$$

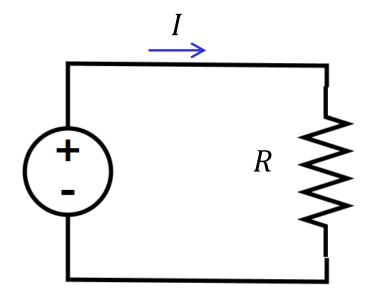
If the resistance  $R_1$  of the first pipe is 2  $\Omega$  and the resistance  $R_2$  of the second pipe is 4  $\Omega$ , the total current I coming out of the source (pump) is:





$$V_S = 8 V$$
 $R_1 = 2 \Omega$ 
 $I = 6 A$ 
 $R_2 = 4 \Omega$ 

**Parallel connection** 

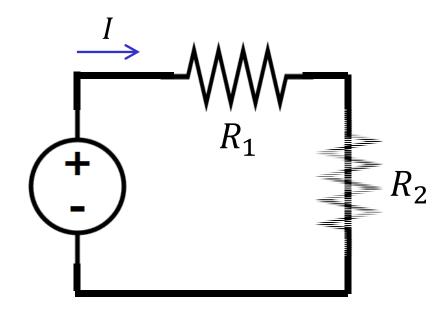


$$V = I \cdot R$$

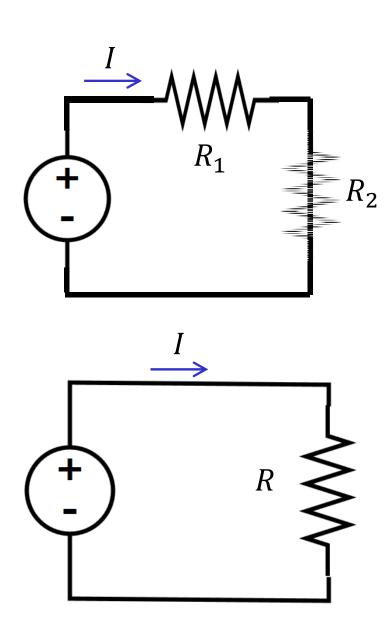
If the resistance  $R_1$  of the first pipe is 1  $\Omega$  and the resistance  $R_2$  of the second pipe is 4  $\Omega$ , the current I coming out of the source (pump) is:

Series connection

$$V_{\rm S} = 10 \ V$$



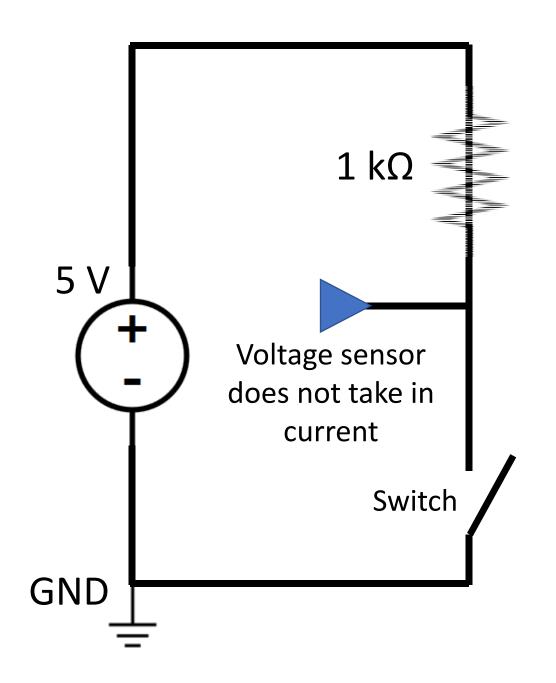
$$V = I \cdot R$$



 $V = I \cdot R$ 

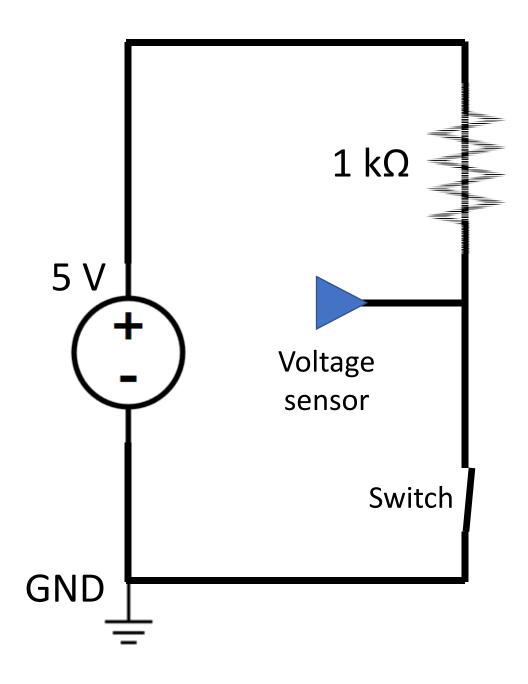
$$V_S = 10 V$$
  
 $R_1 = 1 \Omega$   $I = 2 A$   
 $R_2 = 4 \Omega$ 

Series connection



When the switch is open, the voltage measured by the voltage sensor is:

- [A] 0 V
- [B] 1 mV
- [C] 1 V
- [D] 4 V
- [E] 5 V



When the switch is closed, the voltage measured by the voltage sensor is:

- [A] 0 V
- [B] 1 mV
- [C] 1 V
- [D] 4 V
- **[E]** 5 V

## What did we learn?

- Pipes correspond to resistors, with certain resistance R
- Wires correspond to ideal pipes, with R very small
- Current only flows in a closed loop
- Voltage over an element is what matters
- Current splits in branches
- Voltage gains and drops in a loop have to add to zero
- Ohm's law: V = IR